Essential Question How can you find the volume of a cylinder?

ACTIVITY: Finding a Formula Experimentally

Work with a partner.

- **a.** Find the area of the face of a coin.
- **b.** Find the volume of a stack of a dozen coins.
- c. Write a formula for the volume of a cylinder.





ACTIVITY: Making a Business Plan



Geometry

- In this lesson, you will
- find the volumes of cylinders.find the heights of cylinders given the
- volumes. • solve real-life problems. Learning Standard

8.G.9

Work with a partner. You are planning to make and sell three different sizes of cylindrical candles. You buy 1 cubic foot of candle wax for \$20 to make 8 candles of each size.

- **a.** Design the candles. What are the dimensions of each size of candle?
- **b.** You want to make a profit of \$100. Decide on a price for each size of candle.
- **c.** Did you set the prices so that they are proportional to the volume of each size of candle? Why or why not?

2

ACTIVITY: Science Experiment

Work with a partner. Use the diagram to describe how you can find the volume of a small object.





Consider Similar Problems How can you use the results of Activity 1 to find the volumes of the cylinders?

4 ACTIVITY: Comparing Cylinders

Work with a partner.

- **a.** Just by looking at the two cylinders, which one do you think has the greater volume? Explain your reasoning.
- **b.** Find the volume of each cylinder. Was your prediction in part (a) correct? Explain your reasoning.





-What Is Your Answer?

- 5. IN YOUR OWN WORDS How can you find the volume of a cylinder?
- **6.** Compare your formula for the volume of a cylinder with the formula for the volume of a prism. How are they the same?







"Base times tall, will fill 'em all."



Use what you learned about the volumes of cylinders to complete Exercises 3–5 on page 338.



3 Real-Life Application



So, about 471 cubic centimeters of salsa are missing from the jar.

EXAMPLE

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EXAMPLE

Real-Life Application



About how many gallons of water does the watercooler bottle contain? (1 ft³ \approx 7.5 gal)

(A) 5.3 gallons (B) 10 gallons (C) 17 gallons (D) 40 gallons

Find the volume of the cylinder. The diameter is 1 foot. So, the radius is 0.5 foot.

V = Bh	Write formula for volume.
$=\pi(0.5)^2(1.7)$	Substitute.
$= 0.425\pi \approx 1.3352$	Use a calculator.

So, the bottle contains about 1.3352 cubic feet of water. To find the number of gallons it contains, multiply by the conversion factor $\frac{7.5 \text{ gal}}{1 \text{ ft}^3}$.

$$1.3352\,\text{ft}^3 \times \frac{7.5\,\text{gal}}{1\,\text{ft}^3} \approx 10\,\text{gal}$$

The watercooler bottle contains about 10 gallons of water. So, the correct answer is **B**.

On Your Own

- **3. WHAT IF?** In Example 3, the height of the salsa in the jar is 5 centimeters. How much salsa is missing from the jar?
- 4. A cylindrical water tower has a diameter of 15 meters and a height of 5 meters. About how many gallons of water can the tower contain? (1 $m^3 \approx 264$ gal)



8.1 Exercises





Practice and Problem Solving

Find the volume of the cylinder. Round your answer to the nearest tenth.



12. SWIMMING POOL A cylindrical swimming pool has a diameter of 16 feet and a height of 4 feet. About how many gallons of water can the pool contain? Round your answer to the nearest whole number. (1 $\text{ft}^3 \approx 7.5 \text{ gal}$)

Find the missing dimension of the cylinder. Round your answer to the nearest whole number.

2 13. Volume = 250 ft^3



14. Volume = $10,000 \pi \text{ in.}^3$

15. Volume = $600,000 \text{ cm}^3$



16. CRITICAL THINKING How does the volume of a cylinder change when its diameter is halved? Explain.



17. MODELING A traditional "square" bale of hay is actually in the shape of a rectangular prism. Its dimensions are 2 feet by 2 feet by 4 feet. How many square bales contain the same amount of hay as one large "round" bale?

18. ROAD ROLLER A tank on a road roller is filled with water to make the roller heavy. The tank is a cylinder

that has a height of 6 feet and a radius of 2 feet. One cubic foot of water weighs 62.5 pounds. Find the weight of the water in the tank.

Round hay bale

- **19. VOLUME** A cylinder has a surface area of 1850 square meters and a radius of 9 meters. Estimate the volume of the cylinder to the nearest whole number.
- **20. Problem:** Water flows at 2 feet per second through a pipe with a diameter of 8 inches. A cylindrical tank with a diameter of 15 feet and a height of 6 feet collects the water.
 - **a.** What is the volume, in cubic inches, of water flowing out of the pipe every second?
 - **b.** What is the height, in inches, of the water in the tank after 5 minutes?
 - c. How many minutes will it take to fill 75% of the tank?

Fair Game Review what you learned in previous grades & lessons Tell whether the triangle with the given side lengths is a right triangle. (Section 7.5) 21. 20 m, 21 m, 29 m 22. 1 in., 2.4 in., 2.6 in. 23. 5.6 ft, 8 ft, 10.6 ft 24. MULTIPLE CHOICE Which ordered pair is the solution of the linear system 3x + 4y = -10 and 2x - 4y = 0? (Section 5.3) (A) (-6, 2) (B) (2, -6) (C) (-2, -1) (D) (-1, -2)