

## 2.7 – Dilations (Part 1)

**Essential Questions** - How can you enlarge or reduce a figure in the coordinate plane?

### ACTIVITY 1: Comparing Triangles in a Coordinate Plane

- 1) Work with a partner. Write the coordinates of the vertices of the shaded triangle. Then write the coordinates of the vertices of the nonshaded triangle.

Shaded

$(-2, 1)$

$(2, 2)$

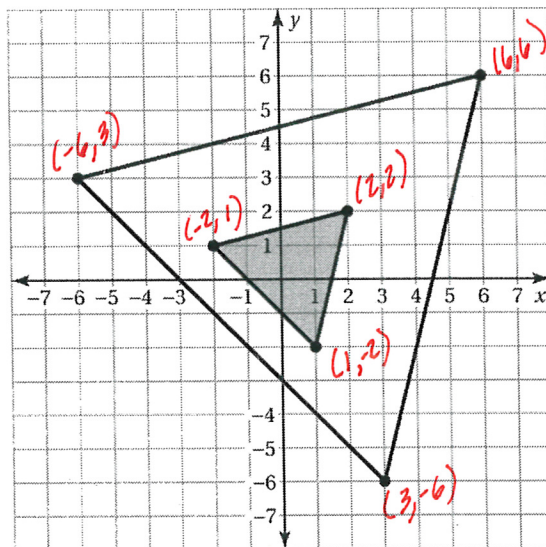
$(1, -2)$

Non-shaded

$(-6, 3)$

$(6, 6)$

$(3, -6)$



- 2) How are the two sets of coordinates related?

The coordinates of the non-shaded triangle are 3 times bigger compared to the shaded triangle.

- 3) How are the two triangles related? **Explain** your reasoning.

The non-shaded triangle is an enlargement of the shaded one due to its size. The triangles are similar due to the fact that sides must be proportional.

- 4) Draw a dashed triangle whose coordinates are twice the values of the corresponding coordinates of the shaded triangle. How are the dashed and shaded triangles related? **Explain** your reasoning.

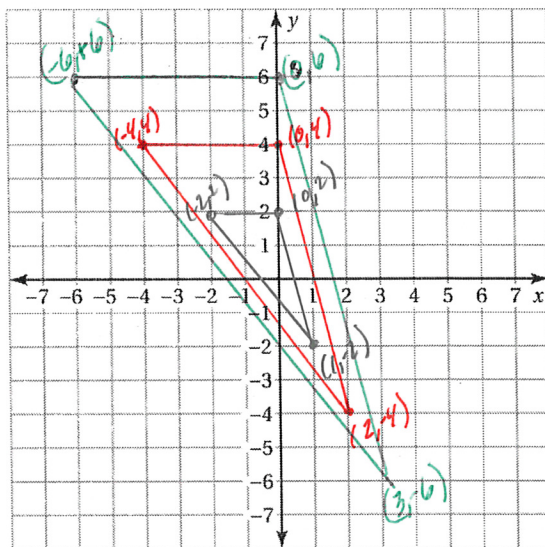
The dashed triangle is the same shape as the shaded triangle, but bigger than the shaded triangle. They are similar triangles.

- 5) How are the coordinates of the nonshaded and dashed triangles related? How are the two triangles related? **Explain** your reasoning.

*The coordinates of the non shaded triangle are multiplied by  $\frac{2}{3}$  to get the dashed triangle. They are similar.*

### **ACTIVITY 2: Drawing Triangles in a Coordinate Plane**

- 6) Draw the triangle whose vertices are  $(0, 2)$ ,  $(-2, 2)$ , and  $(1, -2)$ . Label the vertices on the graph.
- 7) Multiply each coordinate of the vertices by 2 to obtain three new vertices. Draw the triangle given by the three new vertices in a different color and label the new coordinates. How are the two triangles related?



*The new triangle is similar and bigger than the original triangle. It has a scale factor of 2.*

- 8) Repeat #7 by multiplying by 3 instead of 2. Again, use a different color for this and label the coordinates.

### **ACTIVITY 3: Summarizing Transformations**

- 9) Work with a partner. Make a table that summarizes the relationships between the original figure and its image for the four types of transformations (translations, etc.) you studied in this chapter.

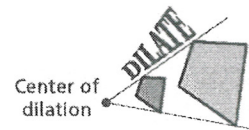
<i>Transformation</i>	<i>Description</i>
<i>Translation</i>	<i>Same size + shape, moved from one place to another</i>
<i>Reflection</i>	<i>Same size + shape, mirror image of the original</i>
<i>Rotation</i>	<i>Same size + shape, rotated around a point</i>
<i>Dilation</i>	<i>Different size, same shape.</i>

- 10) **IN YOUR OWN WORDS**, how can you enlarge or reduce a figure in the coordinate plane if you know the coordinates of the original figure.

*Multiply the original coordinates by a number (the scale factor).*

Complete the following by looking it up in your book.

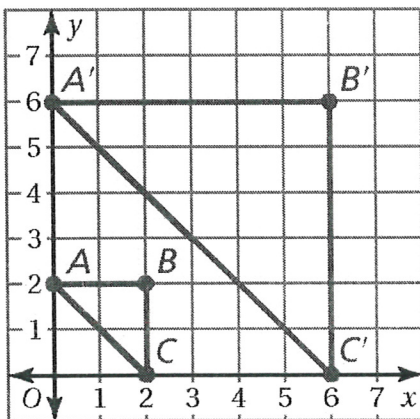
- 11) A dilation is a transformation in which a figure is made **larger** or **smaller** with respect to a point called the center of dilation.



- 12) The ratio of the side lengths of the image to the corresponding side lengths of the original figure is the scale factor of the dilation.
- 13) In other words, the scale factor is the number you multiply to the original coordinates to get the new coordinates.

Complete the following using the image below.

14)



- a) What are the coordinates of the original?

*A(1, 2), B(2, 2), C(2, 1)*

- b) What are the coordinates of the image?

*A'(3, 6), B'(6, 6), C'(6, 3)*

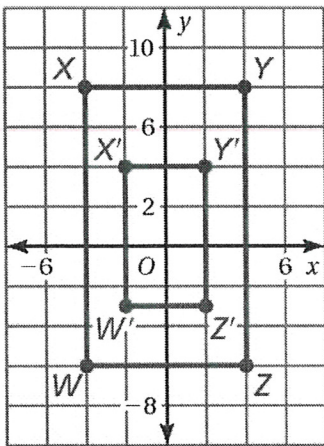
- 15) a) Observe the relationship between the coordinates of the original vertices and the image vertices. What do you believe is the scale factor of the image?

*3*

- b) Is this an enlargement or a reduction?

Complete the following using the image below.

16)



a) What are the coordinates of the original?

$W(-4, -6), X(-4, 8), Y(4, 8), Z(4, -6)$

b) What are the coordinates of the image?

$W'(-2, -3), X'(-2, 4), Y'(2, 4), Z'(2, -3)$

17) a) Observe the relationship between the coordinates of the original vertices and the image vertices. What do you believe is the scale factor of the image?

$\frac{1}{2}$

b) Is this an enlargement or a reduction?

### Summary

18) From you have observed in the last couple of problems, what happens to the original if the scale factor is greater than 1.

*It is enlarged.*

19) From you have observed in the last couple of problems, what happens to the original if the scale factor is less than 1.

*It is reduced.*

20) In your own words, what is a dilation?

*when you enlarge or reduce ~~an~~ a figure in referena to the point of dilation.*