

Name Answers

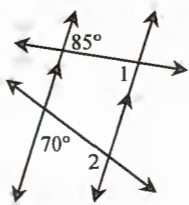
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Chapter 3 & 4 – Final Review

Identify each statement as either true (T) or false (F) by circling the correct choice.

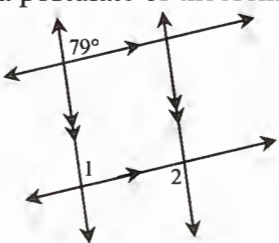
- 1) T **(F)** The slope of a line depends on which points on the line you choose to calculate it.
- 2) T **(F)** If two parallel lines are cut by a transversal then the alternate interior angles are supplementary.
- 3) T **(F)** You can determine the slope of a segment if you are given only the coordinates of its midpoint.
- 4) T **(F)** If ~~any~~ ^{parallel} two lines are cut by a transversal then the alternate exterior angles are congruent.
- 5) **(T)** F If two lines are cut by a transversal forming pairs of congruent corresponding angles, congruent alternate interior angles, or congruent alternate exterior angles, then the lines are parallel.
- 6) **(T)** F If the graph of a line has slope q and y -intercept $(0, r)$ then the equation for the line is $y = qx + r$.
- 7) T **(F)** If lines x, y , and z are in the same plane, and $x \perp y$ and $y \perp z$, then $x \perp z$.
- 8) **(T)** F If two distinct lines on a graph have the same slope, then they are parallel.
- 9) **(T)** F If m is the slope of \overline{AB} , then the slope of the perpendicular bisector of \overline{AB} is $\frac{-1}{m}$.
- 10) **(T)** F If lines x, y , and z are in the same plane, and $x \perp y$ and $y \perp z$, then $x \parallel z$.

For #11 & 12, find $m\angle 1$ and $m\angle 2$. Justify your answer with a postulate or theorem (abbreviations ok).

11) 

$m\angle 1 = 85^\circ$
Reason AIA

$m\angle 2 = 110^\circ$
Reason SSI

12) 

$m\angle 1 = 79^\circ$
Reason CA

$m\angle 2 = 79^\circ$
Reason AIA

- 13) Find the midpoint of the segment connecting points $(3, 5)$ and $(-1, 9)$.

$$x_m = \frac{3 + (-1)}{2} = 1$$

$$y_m = \frac{5 + 9}{2} = 7$$

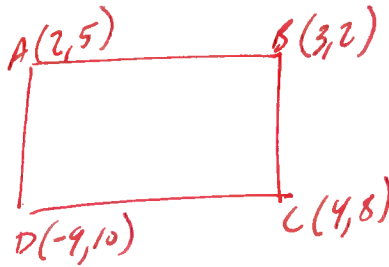
$(1, 7)$

- 14) One endpoint of \overline{AB} is $A(-1, 9)$. The midpoint is $(-3, 6)$. Find the coordinates of the other endpoint.

$(-5, 3)$

- 15) In quadrilateral $ABCD$, with the given coordinates, are the diagonals perpendicular? Show work and explain your reasoning.

$A(2, 5)$
 $B(3, 2)$
 $C(4, 8)$
 $D(-9, 10)$



$$m_{AC} = \frac{3}{2}$$

$$m_{BD} = -\frac{2}{3}$$

Yes, they are \perp because their slopes are opp. reciprocals with each other.

- 16) Write the equation in slope-intercept form of the line through point $B(4, 7)$ and perpendicular to the line: $4x + 2y = 8$.

$$2y = -4x + 8$$

$$y = -2x + 4$$

$$\rightarrow y = \frac{1}{2}x + b$$

$$7 = \frac{1}{2}(4) + b$$

$$7 = 2 + b$$

$$5 = b$$

$$\boxed{y = \frac{1}{2}x + 5}$$

- 17) Write the equation in slope-intercept form of the line that is the **perpendicular bisector** of \overline{AB} . Show all work for full credit.
- 18) What is the equation in slope-intercept form of the line parallel to $y = 2x + 3$ that contains $(4, 6)$?

$A(9, -1)$ and $B(1, 7)$

$$m = \frac{7 - (-1)}{1 - 9} = \frac{8}{-8} = -1$$

$$m_{\perp} = 1$$

$$\text{Midpoint} = \left(\frac{9+1}{2}, \frac{-1+7}{2} \right)$$

$$(5, 3)$$

$$y = 1x + b$$

$$3 = 1(5) + b$$

$$3 = 5 + b$$

$$-2 = b$$

$$\boxed{y = x - 2}$$

$$m = 2$$

$$y = 2x + b$$

$$6 = 2(4) + b$$

$$6 = 8 + b$$

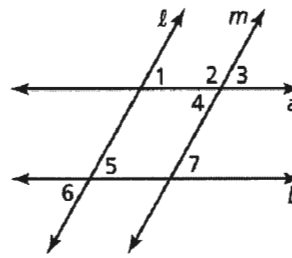
$$-2 = b$$

$$\boxed{y = 2x - 2}$$

Complete the following proof.

- 19) Given: $a \parallel b$
 $\angle 5$ is supplementary to $\angle 2$

Prove: $l \parallel m$



| Statement | Reasons |
|--|---------------------|
| 1. $a \parallel b$ | Given |
| 2. $\angle 5$ is supplementary to $\angle 2$ | Given |
| 3. $\angle 1 \cong \angle 5$ | CA |
| 4. $\angle 1$ is supplementary to $\angle 2$ | Transitive Property |
| 5. $l \parallel m$ | Converse SSI |

- 20) Solve for x and y : (4 pts)

$$-8x + y = -17 \text{ and } 5x - 3y = -6$$

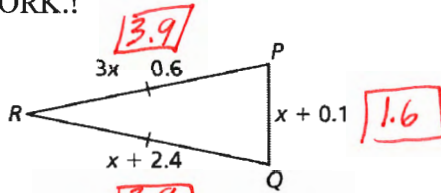
$$\begin{array}{rcl}
 -8x + y & = & -17 \rightarrow -24x + 3y = -51 \\
 5x - 3y & = & -6 \\
 \hline
 -19x & & = -57 \\
 x & = & 3 \\
 y & = & 7
 \end{array}$$

$(3, 7)$

Identify each statement as either true (T) or false (F) by circling the correct choice

- 21) ☒ T ☐ F A triangle with all the sides equal in measure is acute.
- 22) ☒ T ☐ F The capital letters CPCTC are an abbreviation for the phrase "corresponding parts of congruent triangles are congruent."
- 23) ☐ T ☒ F The sum of the measures of the three angles of an obtuse triangle is greater than the sum of the measures of the three angles of an acute triangle.
- 24) ☒ T ☐ F If the base angles of an isosceles triangle each measure 37° , then the vertex angle has a measure of 106° .
- 25) ☐ T ☒ F If a triangle has two angles of equal measure, then the third angle is obtuse.
- 26) ☐ T ☒ F If $\triangle DGO$ is congruent to $\triangle TRA$, then \overline{DG} is congruent to \overline{TA} .
- 27) ☐ T ☒ F The largest side of a triangle is opposite the smallest angle.

- 28) Find the lengths of the missing sides. SHOW WORK.!

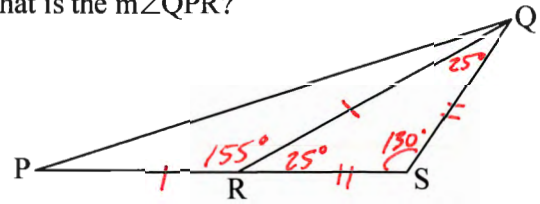


$$3x - 0.6 = x + 2.4$$

$$2x = 3.0$$

$$x = 1.5$$

- 29) $PR = QR$ and $QS = RS$. If the $m\angle RSQ = 130^\circ$, what is the $m\angle QPR$?



$$m\angle QPR = 12.5^\circ$$

- 30) Find the measure of the missing variable.



$$5x - 2 = 2x + 76$$

$$3x = 78$$

$$x = 26^\circ$$

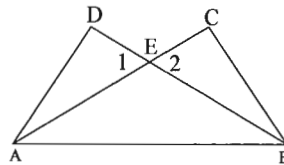
Provide each missing reason or statement in the proof.

- 31) Given: $\angle D \cong \angle C$

$$\overline{DE} \cong \overline{EC}$$

Show: $\overline{AE} \cong \overline{BE}$

Flow-chart Proof:



$$\angle D \cong \angle C$$

Given

$$\overline{DE} \cong \overline{EC}$$

Given

$$\angle DEA \cong \angle CEB$$

VA

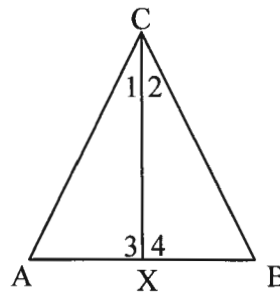
$$\triangle DEA \cong \triangle CEB$$

ASA

$$\overline{AE} \cong \overline{BE}$$

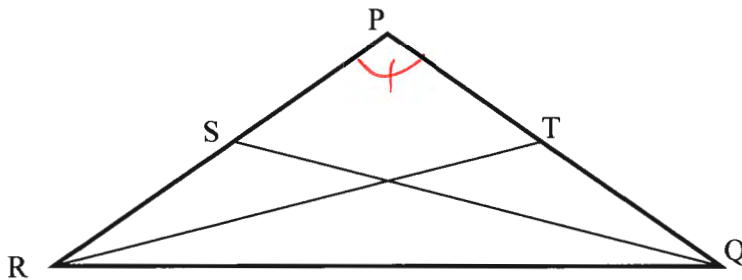
CPCTC

- 32) Given: $\angle 1 \cong \angle 2$
 $\angle 3 \cong \angle 4$
 Prove: $\overline{AC} \cong \overline{BC}$



| Statements | Reasons |
|--|------------------------------|
| 1. $\angle 1 \cong \angle 2$ | 1. <u>Given</u> |
| 2. $\angle 3 \cong \angle 4$ | 2. <u>Given</u> |
| 3. $\overline{CX} \cong \overline{CX}$ | 3. <u>Reflexive Property</u> |
| 4. $\triangle AXC \cong \triangle BXC$ | 4. <u>ASA</u> |
| 5. $\overline{AC} \cong \overline{BC}$ | 5. <u>CPCTC</u> |

- 33) Write a proof.

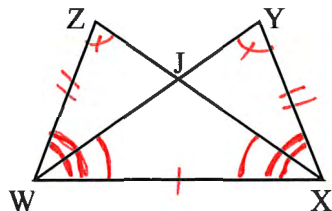


Given: $\overline{PR} \cong \overline{PQ}$
 $\overline{PT} \cong \overline{PS}$

Prove: $\overline{QS} \cong \overline{RT}$

| | |
|-------------------------------------|-----------------|
| $\overline{PR} \cong \overline{PQ}$ | Given |
| $\overline{PT} \cong \overline{PS}$ | Given |
| $\angle RPQ \cong \angle RPQ$ | Reflexive Prop. |
| $\triangle PTR \cong \triangle PSQ$ | SAS |
| $\overline{QS} \cong \overline{RT}$ | CPCTC |

- 34) Given: $\angle ZWX \cong \angle YXW$, $\angle ZXW \cong \angle YWX$
 Prove: $\triangle ZJW \cong \triangle YJX$



$$\angle ZWX \cong \angle YXW$$

Given

$$\angle ZXW \cong \angle YWX$$

Given

$$\overline{WX} \cong \overline{WX}$$

Reflexive

$$\triangle ZWX \cong \triangle YXW$$

ASA

$$\angle Z \cong \angle Y$$

CPCTC

$$\overline{ZW} \cong \overline{YX}$$

CPCTC

$$\angle ZJW \cong \angle YJX$$

VA

$$\triangle ZJW \cong \triangle YJX$$

AAS