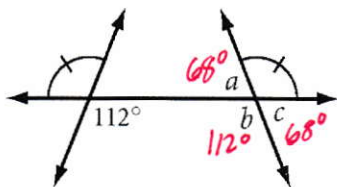


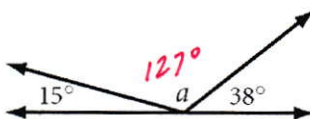
## 2.5 - Proofs About Angle Pairs and Segments (Part 2)

For Exercises 1–8, find each lettered angle measure without using a protractor.

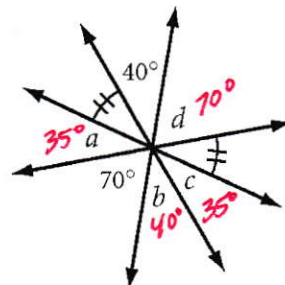
1)



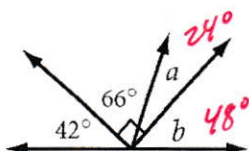
2)



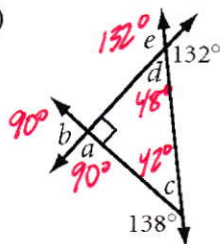
3)



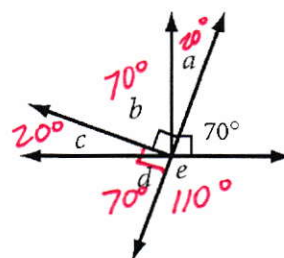
4)



5)



6)



For #7–12, tell whether each statement is always (A), sometimes (S), or never (N) true.

7) The sum of the measures of two acute angles equals the measure of an obtuse angle.

S  $20^\circ + 20^\circ = 40^\circ$

8) If  $\angle XAY$  and  $\angle PAQ$  are vertical angles, then either  $X, A,$  and  $P$  or  $X, A,$  and  $Q$  are collinear.

A

9) The sum of the measures of two obtuse angles equals the measure of an obtuse angle.

N  $91^\circ + 91^\circ = 182^\circ$

10) The difference between the measures of the supplement and the complement of an angle is  $90^\circ$ .

$20^\circ$   $46^\circ$   $70^\circ$

11) If two angles form a linear pair, then they are complementary.

A

12) If a statement is true, then its converse is true.

N

S

For # 13–16, fill in each blank to make a true statement.

13) If one angle of a linear pair is obtuse, then the other is acute.

14) If  $\angle A \cong \angle B$  and the supplement of  $\angle B$  has measure  $22^\circ$ , then  $m\angle A =$   $158^\circ$ .

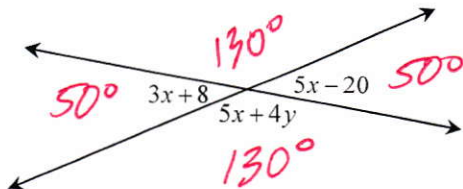
15) If  $\angle P$  is a right angle and  $\angle P$  and  $\angle Q$  form a linear pair, then  $m\angle Q$  is  $90^\circ$ .

16) If  $\angle S$  and  $\angle T$  are complementary and  $\angle T$  and  $\angle U$  are supplementary, then  $\angle U$  is a(n)

obtuse angle.

Find the value of each variable and each angle. SHOW ALL ALGEBRAIC WORK!

17)



$$3x+8=5x-20$$

$$28=2x$$

$$\boxed{14=x} \rightarrow \text{then plug in.}$$

$$5x+4y=130$$

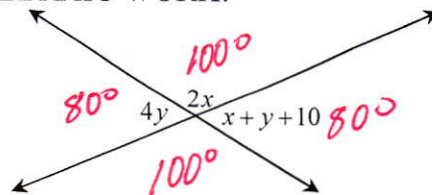
$$5(14)+4y=130$$

$$70+4y=130$$

$$4y=60$$

$$\boxed{y=15}$$

18)



$$2x+4y=180$$

$$2x+(x+y+10)=180$$

$$\rightarrow 2x+4y=180$$

$$3x+y=170$$

$$\rightarrow 2x+4y=180$$

$$-12x-4y=-680$$

$$-10x=-500$$

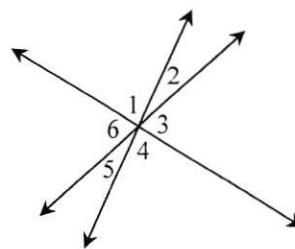
$$\boxed{x=50}$$

$$4y=80$$

$$\boxed{y=20}$$

19) Given:  $\angle 1 \cong \angle 3$

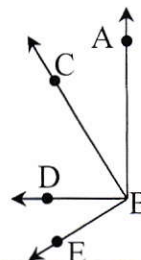
Prove:  $\angle 6 \cong \angle 4$



Statement	Reasons
1. $\angle 1 \cong \angle 3$	Given
2. $\angle 3 \cong \angle 6$	Vertical Angles Th.
3. $\angle 1 \cong \angle 6$	Transitive Property
4. $\angle 1 \cong \angle 4$	Vertical Angles Th.
5. $\therefore \angle 6 \cong \angle 4$	Substitution / Transitive Property

- 20) Given:  $\angle ABD$  is a right angle  
 $\angle CBE$  is a right angle

Prove:  $\angle ABC \cong \angle DBE$



Statement	Reasons
1. $\angle ABD$ is a right angle $\angle CBE$ is a right angle	Given
2. $\angle ABC$ and $\angle CBD$ are complementary	Def of. Comp. Ang.
3. $\angle DBE$ and $\angle CBD$ are complementary	Def of Comp. Ang
4. $\therefore \angle ABC \cong \angle DBE$	Congruent Complements theorem