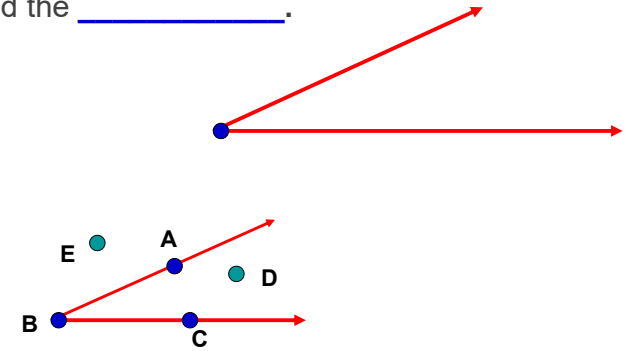


# 1.3 & 1.4

## ANGLES, MEASUREMENT, & ANGLE PAIRS

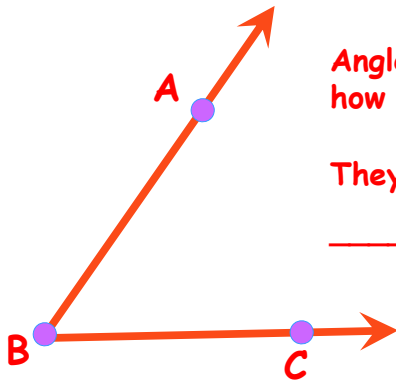
### Angle and Points

- An **angle** is a figure formed by two rays with a common endpoint, called the \_\_\_\_\_.



Points A, B and C are on the angle. D is in the \_\_\_\_\_ and E is in the \_\_\_\_\_.

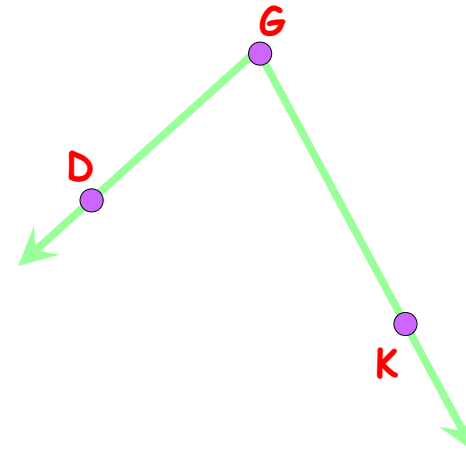
### Measurement of Angles



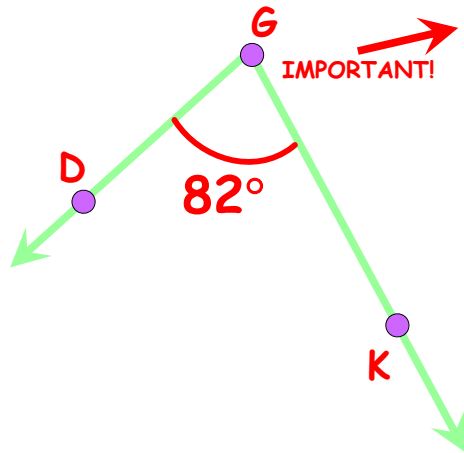
Angles are measured on how open they are.

They're measured by \_\_\_\_\_.

### Naming an Angle



## Naming the measurement of an angle



## Terms to Know

Full Turn  $\rightarrow 360^\circ$

Half Turn  $\rightarrow 180^\circ$

$\frac{1}{4}$  Turn  $\rightarrow 90^\circ$

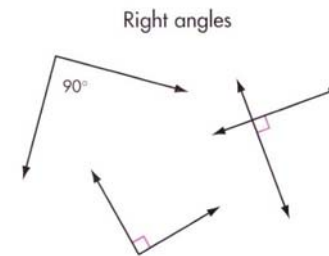
$\frac{1}{8}$  Turn  $\rightarrow 45^\circ$

## WRITING YOUR DEFINITIONS

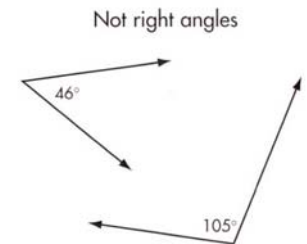
- 1) Precise
- 2) Avoid ambiguous terms (some, about, small...)
- 3) Make sure can't make a counterexample of the definition

## Defining...

1.\* Define *right angle*.



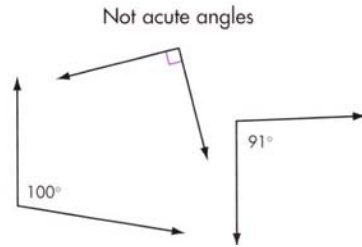
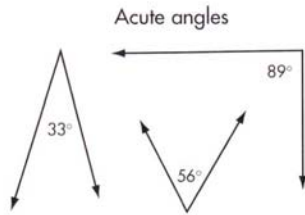
Right angles



Not right angles

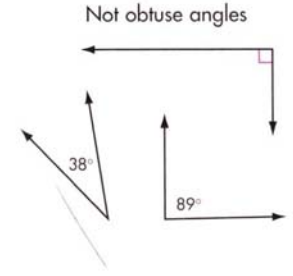
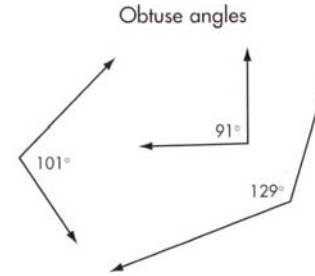
## Defining...

2.\* Define *acute angle*.



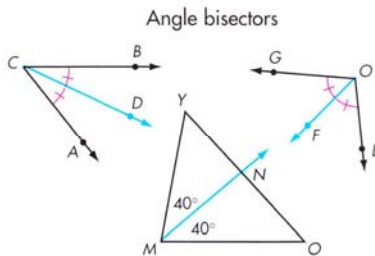
## Defining...

3. Define *obtuse angle*.

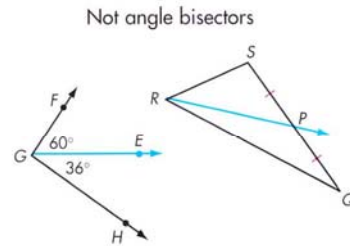


## Defining...

5. Define *angle bisector*.



Ray  $CD$ , ray  $OF$ , and ray  $MN$  are angle bisectors.



Ray  $GE$  and ray  $RP$  are not angle bisectors.

## Adding Angles

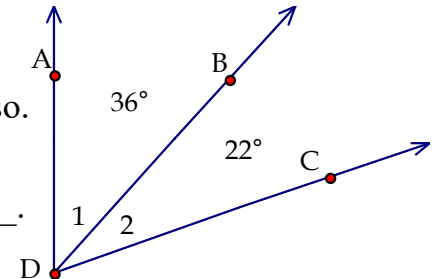
When you want to add angles, use the notation  $m\angle 1$ , meaning the measure of  $\angle 1$ .

If you add  $m\angle 1 + m\angle 2$ , what is your result?

\_\_\_\_\_.

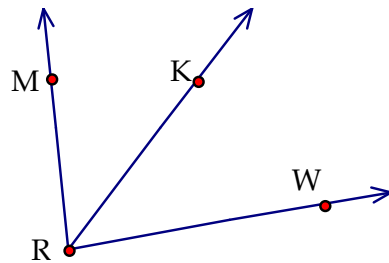
$m\angle 1 + m\angle 2 =$  \_\_\_\_\_ also.

Therefore, \_\_\_\_\_.



# Angle Addition Postulate

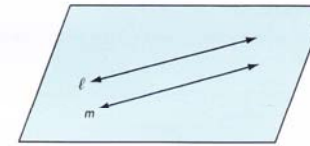
The \_\_\_\_\_ of the two \_\_\_\_\_ will always equal the measure of the \_\_\_\_\_.



$$m \angle \text{---} + m \angle \text{---} = m \angle \text{---}$$

## 1. Define *parallel lines*.

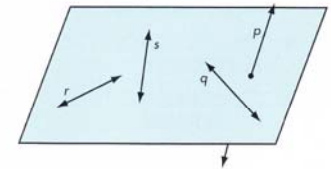
Parallel lines



$$\ell \parallel m$$

Note: Lines are sometimes labeled and named with lowercase letters. The symbol  $\parallel$  means "is parallel to."

Not parallel lines

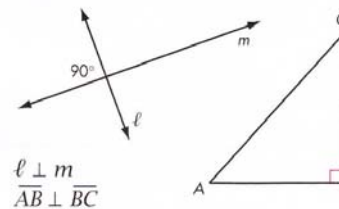


Line  $r$  is not parallel to line  $s$ .  
Line  $p$  is not parallel to line  $q$ .  
Note: Lines  $p$  and  $q$  are not in the same plane. Such lines are called **skew lines**.

# SKEW LINES

## 2. Define *perpendicular lines*.

Perpendicular lines

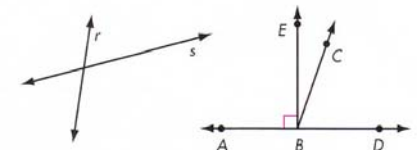


$$\ell \perp m$$

$$\overline{AB} \perp \overline{BC}$$

Note: The symbol  $\perp$  means "is perpendicular to."

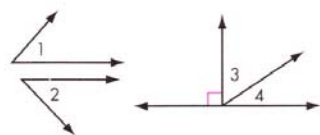
Not perpendicular lines



Line  $r$  is not perpendicular to line  $s$ .  
Ray  $BC$  is not perpendicular to line  $AD$ .

3. Define *pair of complementary angles*.

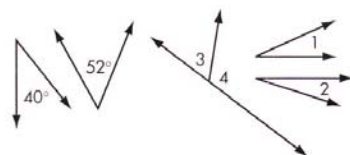
Pairs of complementary angles



$$m\angle 1 + m\angle 2 = 90^\circ$$

$$m\angle 3 + m\angle 4 = 90^\circ$$

Not pairs of complementary angles

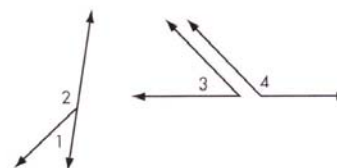


$$m\angle 1 + m\angle 2 < 90^\circ$$

Note: Sometimes it's convenient to name angles in a diagram with a number.

4. Define *pair of supplementary angles*.

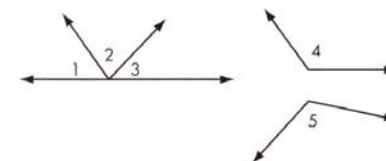
Pairs of supplementary angles



$$m\angle 1 + m\angle 2 = 180^\circ$$

$$m\angle 3 + m\angle 4 = 180^\circ$$

Not pairs of supplementary angles

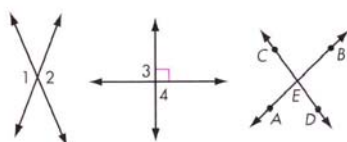


$$m\angle 1 + m\angle 2 < 180^\circ$$

$$m\angle 4 + m\angle 5 > 180^\circ$$

5.\* Define *pair of vertical angles*.

Pairs of vertical angles

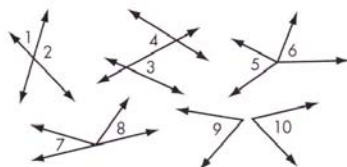


$\angle 1$  and  $\angle 2$  are a pair of vertical angles.

$\angle 3$  and  $\angle 4$  are also vertical angles.

$\angle AED$  and  $\angle BEC$  are also vertical angles.

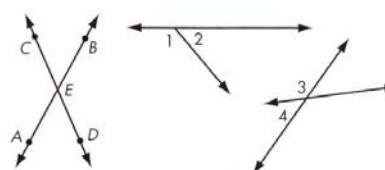
Not pairs of vertical angles



$\angle 1$  and  $\angle 2$ ,  $\angle 3$  and  $\angle 4$ ,  $\angle 5$  and  $\angle 6$ ,  $\angle 7$  and  $\angle 8$ , and  $\angle 9$  and  $\angle 10$  are not pairs of vertical angles.

6.\* Define *linear pair of angles*.

Linear pairs of angles

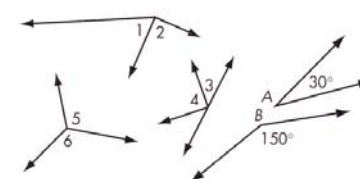


$\angle 1$  and  $\angle 2$  are a linear pair of angles.

$\angle 3$  and  $\angle 4$  are a linear pair of angles.

$\angle AED$  and  $\angle AEC$  are a linear pair of angles.

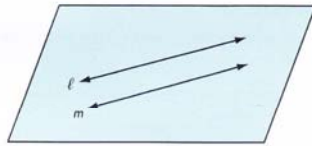
Not linear pairs of angles



$\angle 1$  and  $\angle 2$ ,  $\angle 3$  and  $\angle 4$ ,  $\angle 5$  and  $\angle 6$ , and  $\angle A$  and  $\angle B$  are not linear pairs of angles.

1. Define *parallel lines*.

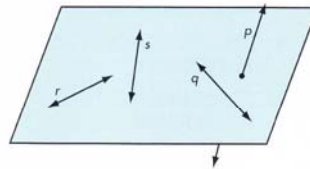
Parallel lines



$\ell \parallel m$

Note: Lines are sometimes labeled and named with lowercase letters. The symbol  $\parallel$  means "is parallel to."

Not parallel lines

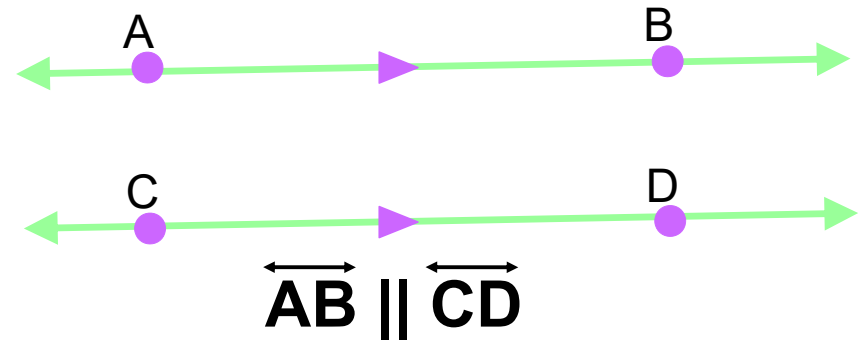


Line  $r$  is not parallel to line  $s$ .  
Line  $p$  is not parallel to line  $q$ .

Note: Lines  $p$  and  $q$  are not in the same plane. Such lines are called **skew lines**.

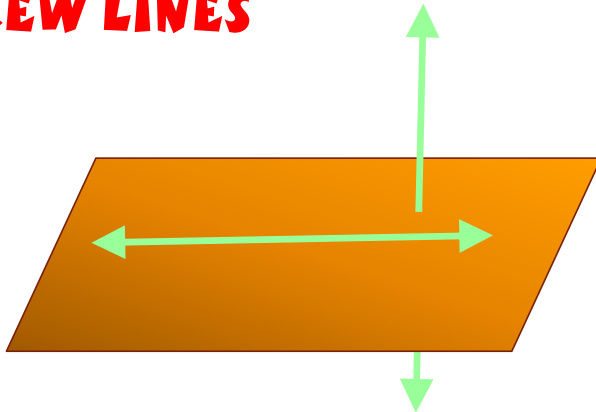
Start  
over

## PARALLEL LINES



Lines that never touch  
and are on the same plane

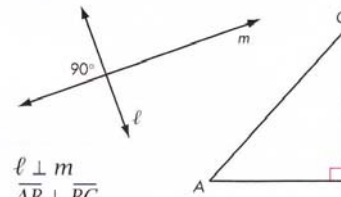
## SKREW LINES



Lines that never touch and  
are on different planes

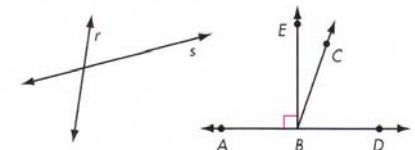
2. Define *perpendicular lines*.

Perpendicular lines



Note: The symbol  $\perp$  means "is perpendicular to."

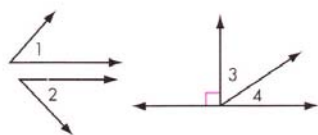
Not perpendicular lines



Line  $r$  is not perpendicular to line  $s$ .  
Ray  $BC$  is not perpendicular to line  $AD$ .

3. Define *pair of complementary angles*.

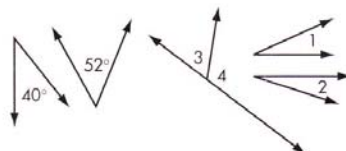
Pairs of complementary angles



$$m\angle 1 + m\angle 2 = 90^\circ$$

$$m\angle 3 + m\angle 4 = 90^\circ$$

Not pairs of complementary angles

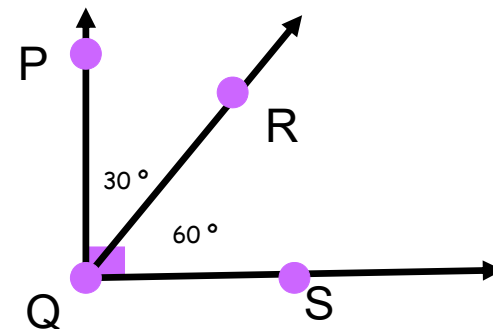


$$m\angle 1 + m\angle 2 < 90^\circ$$

Note: Sometimes it's convenient to name angles in a diagram with a number.

## COMPLEMENTARY ANGLES

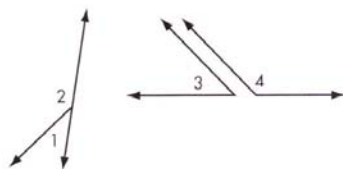
$\angle PQR$  and  $\angle RQS$   
are complementary



Two angles whose sum  
equals  $90^\circ$

4. Define *pair of supplementary angles*.

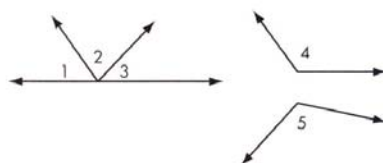
Pairs of supplementary angles



$$m\angle 1 + m\angle 2 = 180^\circ$$

$$m\angle 3 + m\angle 4 = 180^\circ$$

Not pairs of supplementary angles

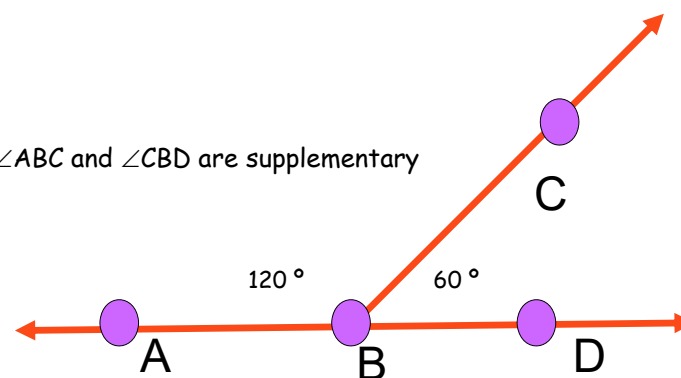


$$m\angle 1 + m\angle 2 < 180^\circ$$

$$m\angle 4 + m\angle 5 > 180^\circ$$

## SUPPLEMENTARY ANGLES

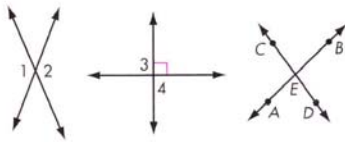
$\angle ABC$  and  $\angle CBD$  are supplementary



Two angles (that don't necessarily  
have to be adjacent) whose sum  
equals  $180^\circ$

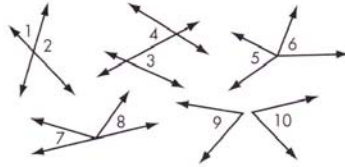
5.\* Define *pair of vertical angles*.

Pairs of vertical angles



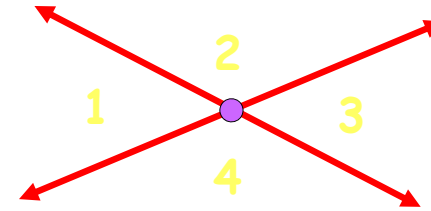
$\angle 1$  and  $\angle 2$  are a pair of vertical angles.  
 $\angle 3$  and  $\angle 4$  are also vertical angles.  
 $\angle AED$  and  $\angle BEC$  are also vertical angles.

Not pairs of vertical angles



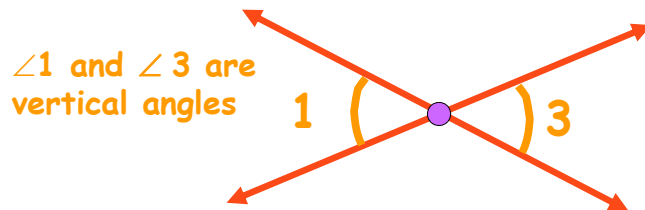
$\angle 1$  and  $\angle 2$ ,  $\angle 3$  and  $\angle 4$ ,  $\angle 5$  and  $\angle 6$ ,  $\angle 7$  and  $\angle 8$ , and  $\angle 9$  and  $\angle 10$  are not pairs of vertical angles.

## VERTICAL ANGLES



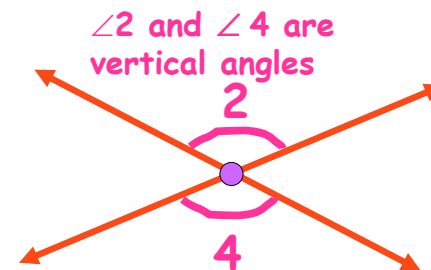
Vertical angles are opposite sides from the vertex when two lines intersect. They are congruent.

## VERTICAL ANGLES



Vertical angles are opposite sides from the vertex when two lines intersect. They are congruent.

## VERTICAL ANGLES

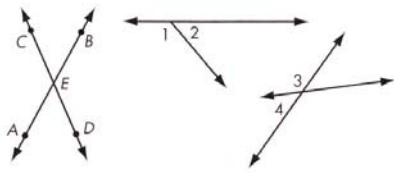


Vertical angles are opposite sides from the vertex when two lines intersect. They are congruent.



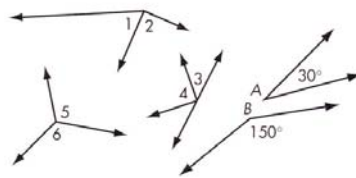
6.\* Define *linear pair of angles*.

Linear pairs of angles



$\angle 1$  and  $\angle 2$  are a linear pair of angles.  
 $\angle 3$  and  $\angle 4$  are a linear pair of angles.  
 $\angle AED$  and  $\angle AEC$  are a linear pair of angles.

Not linear pairs of angles



$\angle 1$  and  $\angle 2$ ,  $\angle 3$  and  $\angle 4$ ,  $\angle 5$  and  $\angle 6$ , and  
 $\angle A$  and  $\angle B$  are not linear pairs of angles.

# Definitions

## Definitions

Point

An undefined term, no size, only location, and 0-D.

Line

Plane

Line Segment

Ray

Collinear